# Known Errors in <br> Discrete Inverse and State Estimation Problems 

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(Special thanks to Dr. Kang Heung Ji, and to several others who communicated these.)
P11 The reference to Eq. (6.1) should be to Eq. (1.20)
P 14 The reference to Eq. (4.35) should be to Eq. (1.26)
P31 line 15: "true estimate" should be "true value"
P37 The 2 in the numerator of Eq. (2.61) should be omitted, and $\sigma^{2}$ in the exponent should be $2 \sigma^{2}$. Thus the equation should be,

$$
p_{r, \phi}(R, \Phi)=\frac{R}{2 \pi} \frac{1}{\sigma^{2}} \exp \left(-R^{2} / 2 \sigma^{2}\right), 0 \leq r,-\pi \leq \phi \leq \pi
$$

P60 line 13: $M+i=1,2, \ldots, N$ should be $i=M+1, M+2, \ldots, N$.
P60 Eq. 2.148 should be $\mathbf{q}=\mathbf{A}_{1}^{-1}\left(\mathbf{b}-\mathbf{A}_{2} \mathbf{r}\right)$
P63 y should be b
P68 Eq. 2.182: = x should be taken out.
P71 line 10: "sidelobes)" should be "sidelobes" without a parenthesis.
P74 2.204: $K+i=1,2, \ldots, M$ should be $i=K+1, K+2, \ldots, M$.
P74 2.205: $K+i=1,2, \ldots, M$ should be $i=K+1, K+2, \ldots, M$.
P74 line 29: $K+i=1,2, \ldots, M$ should be $i=K+1, K+2, \ldots, M$.
P75 2.212: $i>K+1$ should be $i>K$.
P78 2.220: $K+i=1,2, \ldots, M$ should be $i=K+1, K+2, \ldots, M$.
P80 2.233: The upper limit $N$ on the summation should be $M$.
P82 line 26: $\mathbf{I} / \gamma^{2}$ in the left should be $\gamma^{2} \mathbf{I}$.
P83 line 6: Remove 0 at the end, or the upper limit $K$ on the summation would be $M$.
P87 line 9: "a sum of" should be "a linear combination of."
P90 line 13: "and right multiply it by $\mathbf{V}^{\mathrm{T}}$ " should be taken out.
P92 2.293: $\alpha$ in the first term in the second line should be in bold face.
P92 2.293: $\mathbf{Q}_{G}^{\mathrm{T}}$ should be $\mathbf{Q}_{v}^{\mathrm{T}}$.
P104 line 11: $K^{\prime}+i=1,2, \ldots, K$ should be $i=K^{\prime}+1, K^{\prime}+2, \ldots, M$.
P106, 107. The uncertainty should be in terms of $\mathbf{V} \Lambda^{-2} \mathbf{V}^{T}$ rather than $\left(\mathbf{E E}^{T}\right)^{-1}$
P117 line 28: $W=\gamma^{2} I, S=I$ should be $W=I, S^{-1}=\gamma^{2} I$.

P122 Eq. (2.369) $\mathbf{Q}^{-1}$ should be replaced by $\left(\boldsymbol{\Gamma} \mathbf{Q} \boldsymbol{\Gamma}^{T}\right)^{-1}$ and line 11, Eq. (2.352) should be Eq. (2.369)

P128 The first term of the 3rd line of Eq. (2.393) should be $\mathbf{B}\langle\mathbf{y y}\rangle \mathbf{B}^{T}$.
P138 In the first displayed equation of the example, replace $y(1)-y(2)$ by $y(2)-y(1)$.
P140 line 1: $\mathbf{E}(1)$ should be $\mathbf{E}(2)$.
P140 line 29: "a recursive estimation procedure" should be "a recursive minimum variance estimation procedure."

P141 In the first line of Eq. (2.442), the -x term was omitted, so that it should read instead as,

$$
=\left\langle\left(\mathbf{L}_{a}\left(\tilde{\mathbf{x}}_{a}-\mathbf{x}\right)+\left(\mathbf{I}-\mathbf{L}_{a}\right)\left(\tilde{\mathbf{x}}_{b}-\mathbf{x}\right)\right)\left(\mathbf{L}_{a}\left(\tilde{\mathbf{x}}_{a}-\mathbf{x}\right)+\left(\mathbf{I}-\mathbf{L}_{a}\right)\left(\tilde{\mathbf{x}}_{b}-\mathbf{x}\right)\right)^{T}\right\rangle
$$

P146 2.455: $u(\xi) v\left(\xi, \xi_{0}\right)$ should be $u(\xi) \delta\left(\xi_{0}-\xi\right)$.
P147 2.458: $\frac{d}{d \xi}$ in the first term on the left-hand side should be erased.
P147 2.458: $u \frac{\partial^{2} v\left(\xi, \xi_{0}\right)}{\partial \xi^{2}}$ in the second term on the left should be $v \frac{\partial^{2} u\left(\xi, \xi_{0}\right)}{\partial \xi^{2}}$.
P147 2.461: $+\left.u v\right|_{0} ^{L}$ should be $-\left.u v\right|_{0} ^{L}$.
P166 line 1: 2.265 should be 2.264 .
P198 line 24: "Fig. 4.4" should be "Fig. 4.5."
P199 line 22: "Q is multiplied by a large factor to make it visible." is not necessary.
P200 line 2: "Fig. 4.3" should be "Fig. 4.4."
P203 line 4: "Eq. 4.50" should be "Eq. 4.49."
P215 line 34: " 4.71 " should be "4.70."
P220 4.112: $\boldsymbol{\mu}\left(t_{f}\right)$ in the first line and $\mathbf{A}^{\left(t_{f}\right) \mathrm{T}}$ in the second line should be $\boldsymbol{\mu}\left(t_{f}-1\right)$ and $\mathbf{A}^{\left(t_{f}-1\right) \mathrm{T}}$, respectively.

P225 last line: $\mathbf{u}(t)=-[\mathbf{x}(t+1)-\mathbf{x}(t)]$ should be $\mathbf{u}(t)=\mathbf{x}(t+1)-\mathbf{A x}(t)$.
P226 4.126: $\mathbf{Q}(t)^{-1}$ in the second line should be $\mathbf{Q}(t-1)^{-1}$
P226 4.127: $-\mathbf{Q}(t-1)^{-1}$ should be $-\mathbf{Q}(t)^{-1}$.
P232 line 11: "Can controls can be" should be "Can controls be."
P236 line 17: 4.156 should be 4.157 .
P239 4.163: The tilde over $\mathbf{x}_{0}$ in the first line should be omitted.
P240 line 13: 4.156 should be 4.157 .
P240 Eq. (4.164) Delete $\Gamma^{T}$
P241 line 36: 4.156 should be 4.157 .
P266 line 11: $\mathbf{R}=\operatorname{diag}([1,0])$ should be $R=1$.
P271 5.19 should be $\hat{\mathbf{x}}(s)=\left(\mathbf{I}-\mathbf{e}^{-2 \pi i s} \mathbf{A}\right)^{-1} \hat{\mathbf{q}}(s)$ with subsequent redefinition of the resolvent.

P274 line 10: $\mathbf{N}_{1}=\mathbf{Q}$ should be $\mathbf{N}_{1}=\mathbf{B}_{1}$.

Please report further errors to cwunsch@mit.edu

